Your version is $\square \mathbf{Z} \square \square \square$. Please copy your version into your answer form. Please answer the questions first here (and on the scratch paper). Copy your answers only at the end into the answer form. You will return only the answer form, you will keep this task sheet. Good luck!

Question: Demand and supply are given by $Q_{D}=16-2 P-P^{2}$ and $Q_{S}=2 P+P^{2}$. What is the price in equilibrium? (assume that the price must be positive) (2 points)

1: \begin{tabular}{|c|c|c|c|c|c|}

\hline | other |
| :---: |
| value | \& | b |
| :--- |
| v |$+\sqrt{7}$ \& c \& 2 \& $8 / 3$ \& 8 \\

\hline
\end{tabular}

Question: $\quad$ Be $f=4 x^{2}+9$. What is $f^{\prime}(3)$ ?

2: \begin{tabular}{|c|c|c|c|c|c|c|}

\hline | a |
| :---: |
| other <br> value |
| b | \& $8 x$ \& ${ }^{\text {b }}$ \& 24 \& d points) \& $4 x^{2}$ \& $e^{\text {e }}$ \\

\hline
\end{tabular}

Question: Find the derivative of
$\frac{2}{3} x^{3}+x^{2}+2 x+7$
(1 points)
3a: None of the following is correct.
3b: $2 x^{2}+2 x+2$
3c: $\frac{2}{3} x^{2}+2 x+2$
3d: $\frac{3}{x}^{2}+2 x+2$
3e: $\frac{2}{3} x^{2}+x+2$

Question: Find the derivative of $\left(x^{2}-2 x+3\right)^{17} \quad$ (2 points)
4a: None of the following is correct.
4b: $17\left(x^{2}-2 x+3\right)^{16}$
4c: $16\left(x^{2}-2 x+3\right)^{17}$
4d: $16(2 x-2)\left(x^{2}-2 x+3\right)^{17}$
4e: $17(2 x-2)\left(x^{2}-2 x+3\right)^{16}$

Question: Find the derivative of $\left(x^{2}+\right.$
4) $x^{-1}$
(1 points)

5: \begin{tabular}{|c|c|c|c|c|c|}

\hline a | other |
| :---: |
| value | \& $\frac{x^{2}-4}{x^{2}}$ \& \& $2 x$ \& $\frac{x^{2}+4}{x^{2}}$ \& $\frac{e}{c} \frac{x^{2}+4}{x}$ \\

\hline
\end{tabular}

Question: Be $y=4 x^{5}+3 x^{3}+3 x$. What is $d x / d y$ ?
(2 points)
6a: None of the following is correct.
6b: $20 y^{4}+9 y^{2}+3$
6c: $20 x^{4}+9 x^{2}+3$
6d: $1 /\left(20 x^{4}+9 x^{2}+3\right)$
6e: 0

Question: If $f^{\prime}(x)=\frac{x-1}{x+1}$, what is $f^{\prime \prime}(x)$ ?

7: | $\begin{array}{l}\text { other } \\ \text { value }\end{array}$ | $-\frac{x-1}{(x+1)^{2}}$ | c | $\frac{2}{x+1}$ | $\mathrm{~d}^{\mathrm{d}} \frac{2}{(x+1)^{2}}$ | ${ }^{\mathrm{e}} \frac{1}{x+1}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |

Question: If $f^{\prime}(x)=e^{-2 x^{2}+3 x+4}$, what is $f^{\prime \prime}(x)$ ?
(1 points)
8a: None of the following is correct.
8b: $\left(-2 x^{2}+3 x+4\right) e^{-2 x^{2}+3 x+4}$
8c: $e^{-2 x^{2}+3 x+4}$
8d: $\left(-2 x^{2}+3 x+4\right) e^{3-4 x}$
8e: $(3-4 x) e^{-2 x^{2}+3 x+4}$
Question: Be $f(x)=-x^{3}+\frac{9}{2} x^{2}-6 x+6$. Where does $f(x)$ have a local maximum?
(3 points)

9: \begin{tabular}{|c|c|c|c|c|c|c|c|}

\hline | other |
| :---: |
| value | \& 1 \& \& \& \multicolumn{1}{c}{ (3 points) } \\

\hline
\end{tabular}

Question: Be $f(x, y)=-y^{2}-2 a x y+$ $2 x^{2}$. What is the value of $f_{x y}(3,1)$ ?

10: | a other |
| :---: | :---: | :---: | :---: | :---: | :---: |
| value | $\mathrm{b}^{\mathrm{b}}-2 a \mathrm{c}^{\mathrm{c}} \quad 3 \mathrm{~d}$ points)

Question: $\operatorname{Be} f(x, y)=\frac{x^{2}-1}{x y}$. What is the value of $f_{x y}(3,1)$ ?


Question: Be $f^{\prime}=-2 x^{2}+10 x-12$. For which value of $x$ does $f$ have a maximum?
(2 points)

12: \begin{tabular}{|l|l|l|l|l|}
\hline a \(\begin{array}{c}other \\

value\end{array}\) \& | $b$ |
| :--- |
| $x=\sqrt{37}$ |${ }^{c} x=2$ \& ${ }^{d} x=\frac{5}{2}$ \& ${ }^{e} x=3$ \\

\hline
\end{tabular}

Question: A two-product firm faces the following demand and cost functions: $\mathrm{Q}_{1}=24-2 \mathrm{P}_{1}-\mathrm{P}_{2} ; \quad \mathrm{Q}_{2}=24-\mathrm{P}_{1}-$ $2 \mathrm{P}_{2} ; \quad \mathrm{C}=\mathrm{Q}_{1}^{2}+3 \mathrm{Q}_{2}^{2}+10$. Which value of $P_{2}$ satisfies the first-order condition to maximise profit?

13: \begin{tabular}{|c|c|c|c|c|c|}

\hline | other |
| :---: |
| value | \& \& \& \& (5 points) \\

\hline
\end{tabular}

Question: Maximise $x \cdot(y-4)$ subject to the constraint $x+y=6$. Which value for $x$ satisfies the first-order condition?


Question: Maximise $x+y$ subject to the constraint $x^{2}+y^{2}=2$. Which positive value for $x$ satisfies the first-order condition?
(5 points)

$15:$| aother <br> value | 1 | $b^{b}$ | 2 | d | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |

Question: Find $\int \frac{x-1}{x+1} d x$
(3 points)
16a: None of the following is correct.
16b: $\left(x^{2} / 2-x\right) /\left(x^{2} / 2+x\right)+C$
16c: $\left(x^{2} / 2-x\right) \ln (x+1)+C$
16d: $x-\ln (x+1)+C$
16e: $x-2 \ln (x+1)+C$

Question: Find $\int_{e}^{3} \frac{x+1}{x-1} d x$
(3 points)
17a: None of the following is correct.
17b: $-2 \ln (e-1)+2 \ln 2-e+3+C$
17c: $2 \ln (x-1)+x+C$
17d: $\frac{x+2}{x-2}+C$
17e: $5-\frac{e+2}{e-2}+C$

Question: What is the value of $\int_{3}^{0} f(x) d x$ if $F(x)=-2 x+5$ ?


Question: Be $u>1$ and $f(x)=\ln (x)$, what is $\frac{d}{d u} \int_{1}^{u} f(x) d x$ ?


Question: Find $\int_{1}^{2} e^{2 x+1} d x$

20: | $\begin{array}{c}\text { other } \\ \text { value }\end{array}$ | $\frac{b_{5}}{3}\left(e^{5}-e^{3}\right)$ | $\frac{1}{2}\left(e^{5}-e^{3}\right)$ | ${ }^{\text {d }} e^{5}-e^{3}$ | ${ }^{e} \frac{1}{2} e^{2 x+1}$ |
| :--- | :--- | :--- | :--- | :--- |

total number of points: 47
obtainable through randomisation: 10 sufficient to pass: 23

